

# Branes in cosmology and colliders

Jose A. R. Cembranos



Fine Theoretical Physics Institute



UNIVERSITY OF MINNESOTA

Work done in collaboration with  
Antonio Dobado, Antonio L. Maroto  
Juan Alcaraz, Salvatare Melle,  
Marat Gataullin, Louis Strigari,  
Alvaro de la Cruz Dombriz,...



**Santa Fe 2010 Summer Workshop**

**“LHC: From Here to Where?”**

July 5 - July 9, 2010

# CONTENTS

---

## 1.- Extra Dimensions

→ 1.a. Brane Models

## 2.- Branons

2.a. Effective Action

2.b. Particle Colliders

2.c. Cosmology and  
Astrophysics

2.d. Radiative  
Corrections

# SPAIN WON

- Spain is in the final!!!



# SAN FERMÍN

○ TODAY IS SAN FERMIN!!!!!!

○ 07/07

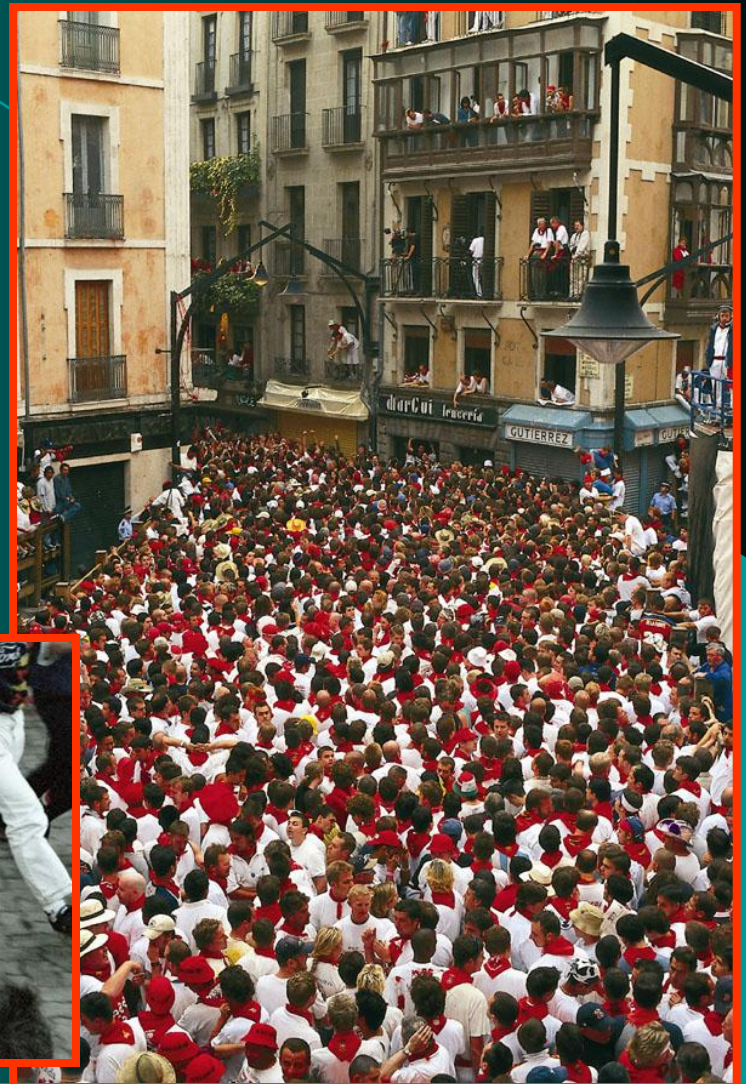


Pamplona



# SAN FERMÍN

- TODAY IS SAN FERMIN!!!!
- 07/07
- El encierro: The bulls walk from the stable to the Plaza de Toros, where next day, they will fight against the toreto (bull-fighter).
- They run 900 meters approx.



Pamplona

# EXTRA DIMENSIONS

The main motivations for considering extra dimensions have a theoretical origin.

In the last years the most part of the development in theoretical physics required the introduction of extra dimensions (ED):

- 1.- Modern Kaluza-Klein (KK) Theories
- 2.- Supersymmetry (SUSY) and Supergravity (SUGRA)
- 3.- Superstrings
- 4.- M-Theory

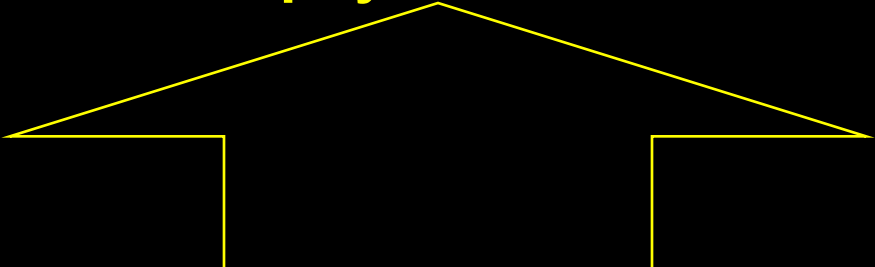
**Introduction of new ideas related to  
non-perturbative effects : BRANES**



# BRANE WORLDS (BW)

---

**Detectable extra dimensions.  
Possible new physics at the TeV scale**



**New scenarios where resolving the hierarchy problem:      **Brane Worlds (BW)****

ADD Model (Arkani-Hamed, Dimopoulos and Dvali, 1998)

RS Models (Randall and Sundrum, 1999)    ...

# THE RESTRICTED UNIVERSE

The main idea is that our universe is restricted to a 3-brane embedded in a higher  $D$  dimensional space, with  $D = 4 + \delta$ , being the  $\delta$  extra dimensions compactified..

In this picture the Standard Model (SM) particles are confined to the 3-brane but gravitons can propagate along the whole bulk space.





# ADD HIERARCHY

The fundamental scale of gravity is  $M_F$ , which could be of the order of the electroweak scale in order to solve the hierarchy problem:

$$M_F \simeq 1 \text{ TeV}$$



$$M_P^2 = V_\delta M_F^{2+\delta}$$

The hierarchy between the Planck and electroweak scale is generated by the large volume of the extra dimensions

The typical size  $R$ , of the extra dimensions ranges from a fraction of  $mm$  for  $\delta=2$  to about  $10 F$  for  $\delta=7$ .

# BRANE WORLD SIGNALS

## 1.- New Gravitation:

Newton law deviations

KK gravitation

Black

New physics at the  $M_F$  scale  
 $M_F$ : Fundamental gravitation scale in  $D$   
dimensions ( $M_P^2 = V_\delta M_F^{D-2}$ )

## 2.- The brane as a new dynamical object:

Branons = Brane fluctuations

Topological brane configurations

String

Brane

New physics at the  $f$  scale  
 $f$ : Brane tension scale  
( $\tau = f^4$ )

Trapped States

# BRANE FLUCTUATIONS

Rigid objects do not exist in relativistic theories.

Consequences of the brane oscillations:

1.- **Branons**: New fields which represent the position of the brane in the bulk space.

These fields are the (pseudo-)Goldstone bosons corresponding to the spontaneous symmetry breaking of the translation invariance produced by the presence of the brane.

2.- **KK coupling suppression** : The KK modes decouple from the SM particles (on the brane)

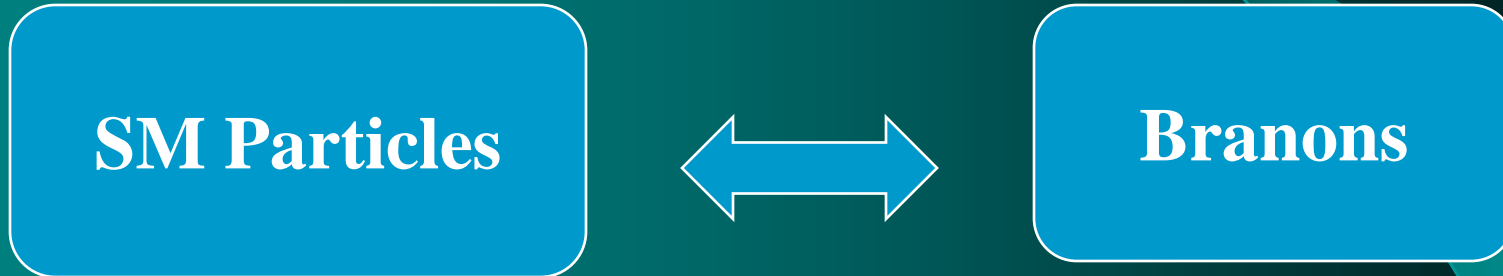
$f \ll M_F$  : The KK modes decouple from the SM particles (on the brane)

$$g \sim g \cdot e^{-\frac{1}{2} \left( \frac{m}{R} \right)^2} \sim \frac{M_F^2}{f^4}$$

(Bando, Kugo, Noguchi and Yoshioka)

# BRANONS AND THE SM PARTICLES

The conclusion is that for flexible branes ( $f \ll M_F$ ), the only relevant degrees of freedom at low energies in the ADD scenario are the SM particles and the branons.



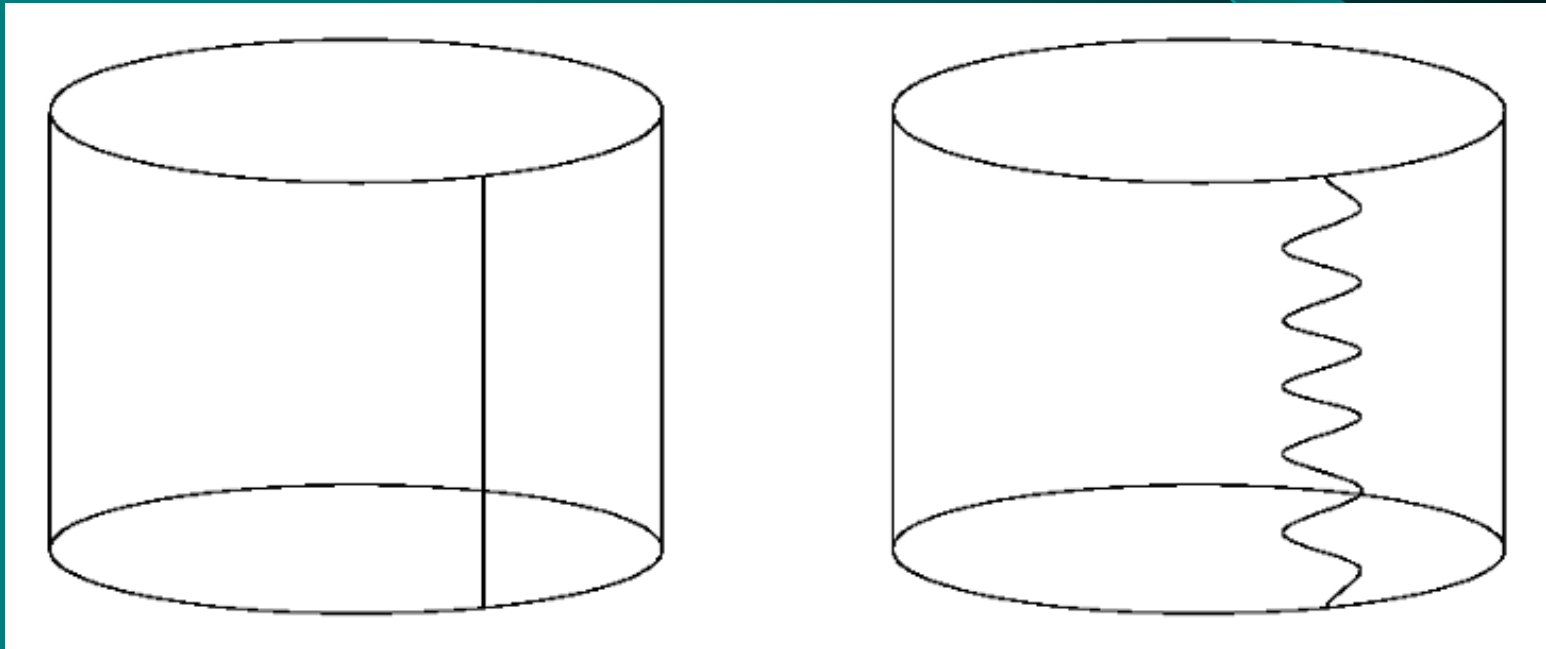
Branons, as Goldstone or pseudo-Goldstone bosons, are expected to be weakly interacting at low energies (compared with  $f$ ).



Description through an  
EFFECTIVE LAGRANGIAN

# LOWER DIMENSIONAL EXAMPLE

Brane with trivial topology. The ground state of the brane is represented on the left. On the right we plot an excited state.





# BRANON FIELD

Brane coordinates

Bulk Metric:

$$G_{MN} = \begin{pmatrix} \tilde{g}_{\mu\nu}(x) & 0 \\ 0 & -\tilde{g}'_{mn}(y) \end{pmatrix}$$

Induced  
Metric:

Extra dimensional coordinates

$$g_{\mu\nu} = \partial_\mu Y^M \partial_\nu Y^N G_{MN} = \tilde{g}_{\mu\nu} - \partial_\mu Y^m \partial_\nu Y^n \tilde{g}'_{mn}$$

Branon  
fields

$$Y^m(x) = Y^m(Y_0, \pi^\alpha(x)) = Y_0^m + \frac{1}{\kappa f^2} \xi_\alpha^m(Y_0) \pi^\alpha(x) + \mathcal{O}(\pi^2)$$

$$\kappa^2 = 16\pi/M_P^2$$

$\xi_a$

Killing vectors corresponding to translations on the extra space.

# BRANON NLSM

At low energies the dominant term in the brane action is the Nambu-Goto term:

$$S_B = -f^4 \int_{M_4} d^4x \sqrt{g}$$

Expanding in branon fields, the dominant term at low energies is a Non-Linear Sigma Model for branons defined on the coset space (or equivalent extra space, if it is homogeneous).

Formally very similar to chiral lagrangians in QCD

$$S_B^{(2)} = -\frac{f^4}{2} \int_{M_4} d^4x \sqrt{\tilde{g}} \tilde{g}^{\mu\nu} h_{\alpha\beta}(\pi) \partial_\mu \pi^\alpha \partial_\nu \pi^\beta$$

# BRANON MASSES

The branons acquire mass in a more general case, when the translational isometries of the extra space are only approximated.

$$G_{MN} = \begin{pmatrix} \tilde{g}_{\mu\nu}(x, y) & 0 \\ 0 & -\tilde{g}'_{mn}(y) \end{pmatrix}$$

This fact is related to non factorizable metrics.

$$\sqrt{g} = 1 - \frac{1}{2f^4} \eta^{\mu\nu} \delta_{\alpha\beta} \partial_\mu \pi^\alpha \partial_\nu \pi^\beta + \frac{1}{2f^4} M_{\alpha\beta}^{(2)} \pi^\alpha \pi^\beta + \dots$$

# SM INTERACTIONS

The interaction of the branons with the SM particles is given by:

$$S_B = \int_{M_4} d^4x \sqrt{g} [-f^4 + \mathcal{L}_{SM} - M_{\alpha\beta}^2 \pi^\alpha \pi^\beta \eta_{\mu\nu}] T_{SM}^{\mu\nu}(\eta_{\mu\nu}) \Big] + \mathcal{O}(\pi^3).$$

**N: Number of branons.**  
**M: Branon mass.**  
**f: Brane tension scale.**

As in the case of the gravitons, the branons couple to the SM through:

$$T_{SM}^{\mu\nu} = - \left( \tilde{g}^{\mu\nu} \mathcal{L}_{SM} + 2 \frac{\delta \mathcal{L}_{SM}}{\delta \tilde{g}_{\mu\nu}} \right) \Big|_{\tilde{g}_{\mu\nu} = \eta_{\mu\nu}}$$

(Sundrum, Creminelli and Strumia)

# PARTICLE COLLIDERS

## 1.- Electroweak bosons widths modifications.

- 2.a. Invisible Z width.
- 2.b. W decay.

## 2.- Direct searches in $e^+e^-$ colliders.

- 2.a. Single photon channel.
- 2.b. Single Z channel.
- 2.c. Prospects for future LC.

## 3.- Direct searches in hadronic colliders.

- 3.a. Single photon channel.
- 3.b. Mono jet channel.
- 3.c. Prospects for future hadronic colliders.



# Z AND W DECAYS

## Restrictions from LEP-I (plot for $N = 1$ ):

### 1.- Z invisible width:

$$\Delta\Gamma_Z^{\text{inv.}} < 2.0 \text{ MeV (LEP I)}$$

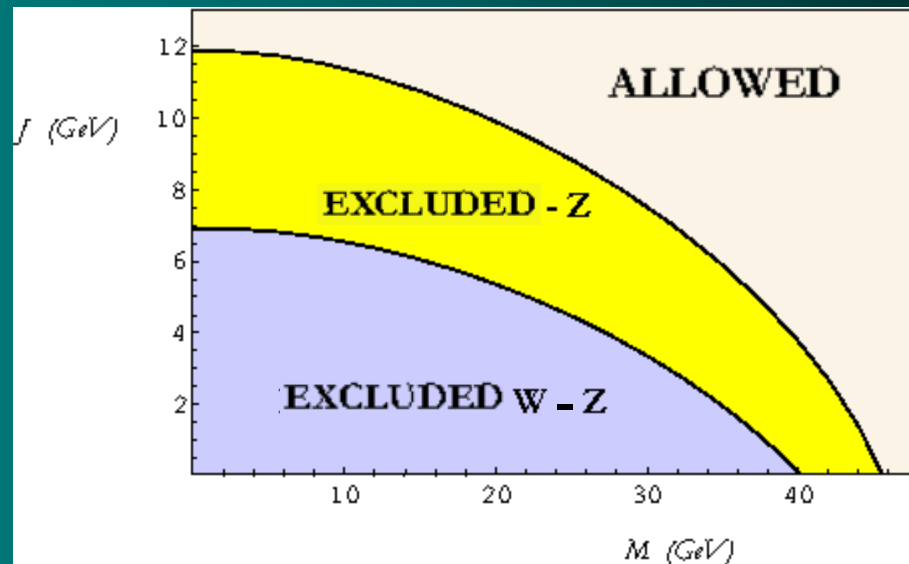
$$\Gamma_Z^b: Z \longrightarrow \bar{\nu}(p_1)\nu(p_2)\pi(k_1)\pi(k_2)$$

### 2.- W total width:

$$\Delta\Gamma_W^{\text{total}} < 240 \text{ MeV (LEP I)}$$

$$\Gamma_W^b: W^- \longrightarrow l^-(p_1)\bar{\nu}(p_2)\pi(k_1)\pi(k_2)$$

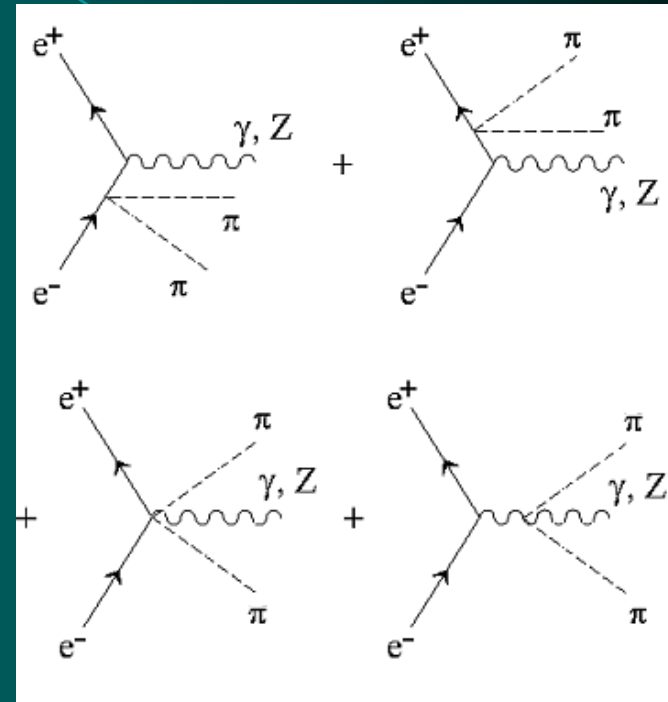
$$W \longrightarrow q(p_1)\bar{q}(p_2)\pi(k_1)\pi(k_2)$$



# SINGLE $\gamma$ AND Z CHANNELS

$\gamma$  or Z production

A more important experimental signal is associated to the single photon channel (or single Z channel) plus missing energy.



$$\frac{d\sigma_A}{dx d\cos\theta} = \frac{|h|^2 s(c_V^2 + c_A^2)(s(1-x) - 4M^2)^2 N}{4\pi \cdot 61440 f^8 \pi^2} \sqrt{1 - \frac{4M^2}{s(1-x)}} \left[ x(3 - 3x + 2x^2) - x^3 \sin^2\theta + \frac{2(1-x)(1 + (1-x)^2)}{x \sin^2\theta} \right]$$

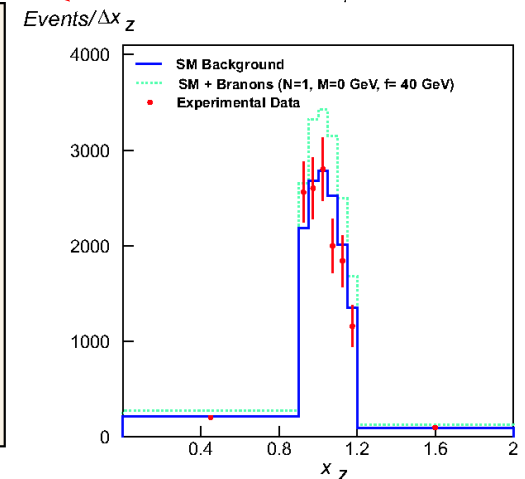
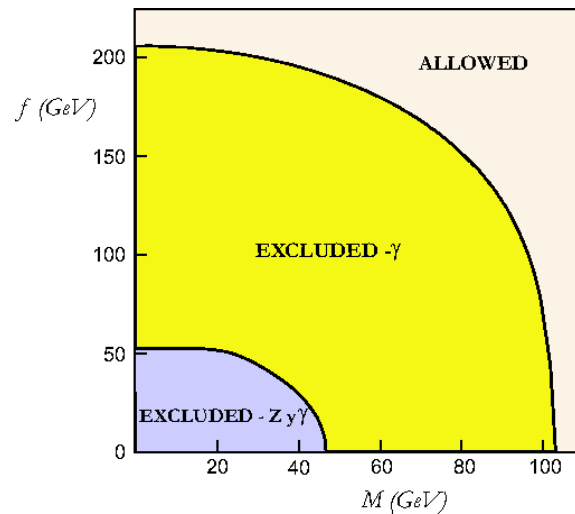
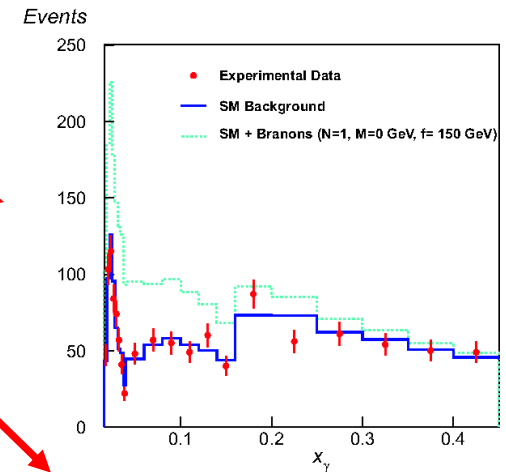
# L3 DATA ANALYSIS

L3 is a collaboration with more than 50 institutions from all the world.

L3 was a detector working with the produced particles in the electron-positron collisions in the LEP ring (CERN).

## Analysis:

- 1.- Single photon
- 2.- Single Z
- 3.- Restrictions



# LC PROSPECTS

To estimate the future linear colliders sensitivity, we have take into account the statistics improuve due to the total integrated luminosity ( $\mathcal{L}$ ) difference:

$$\sigma_{TII}^i = \sqrt{\frac{\mathcal{L}_{TII}}{\mathcal{L}_{TI}}} \sigma_{TI}^i$$

1.- Medium time.

1.- ILC

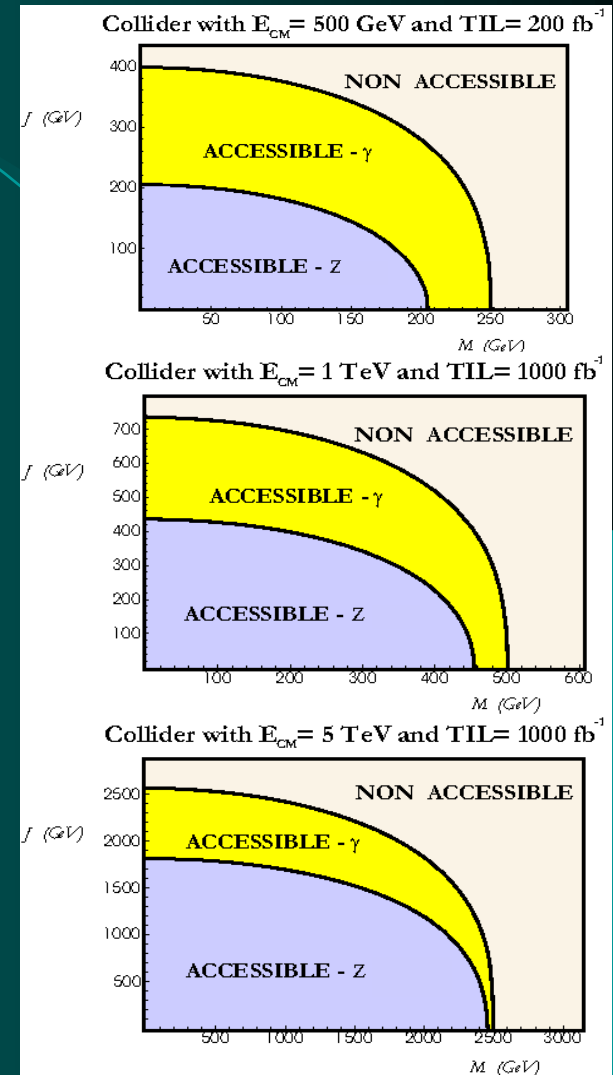
1.a.  $E_{CM} = 500$  GeV

1.b.  $E_{CM} = 1$  TeV

2.- Long time

2.- CLIC

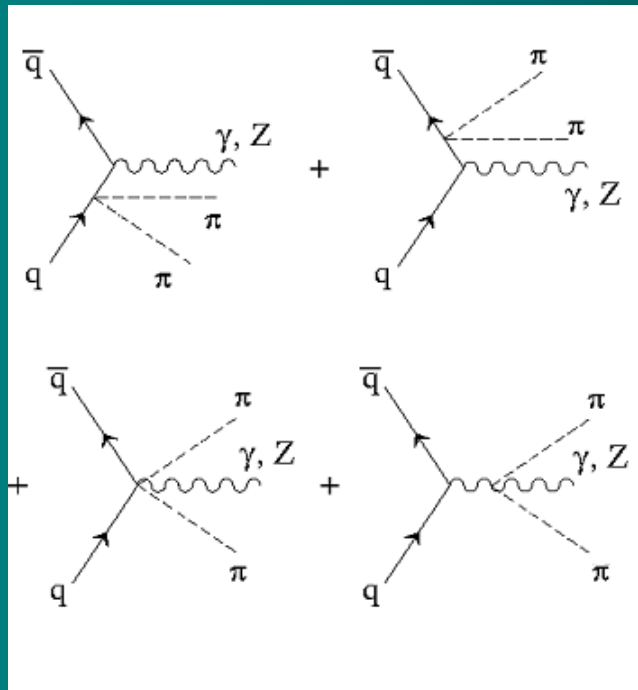
2.a.  $E_{CM} = 5$  TeV



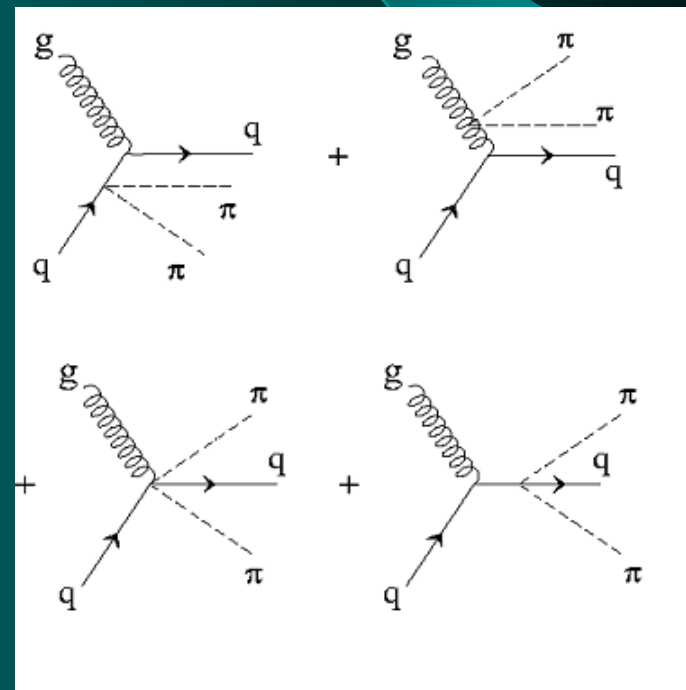
# HADRONIC COLLIDERS

The main experimental signals come from the single photon channel (or electroweak boson) and the monojet production plus missing energy and transversal momentum.

One  $\gamma$  or  $Z$  production



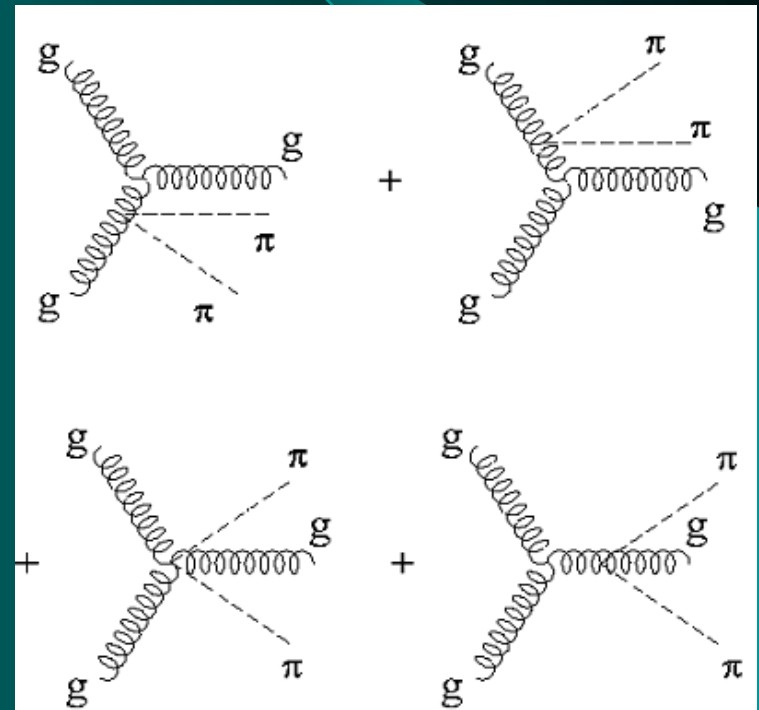
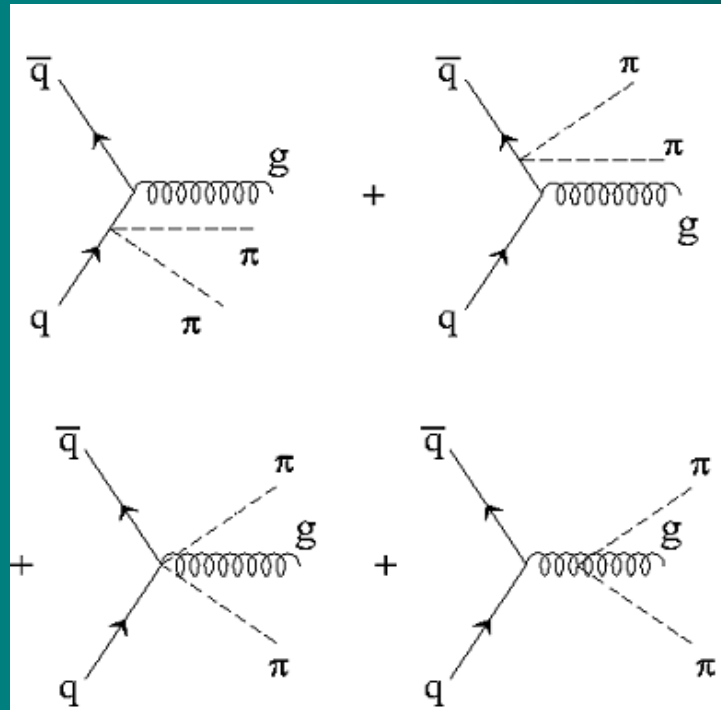
One quark production





# GLUON PRODUCTION

## Gluon production



# TEVATRON RESULTS

Tevatron is a collider  
proton-antiproton  
placed in the *Fermi  
National Laboratory  
Accelerator*  
(Chicago)

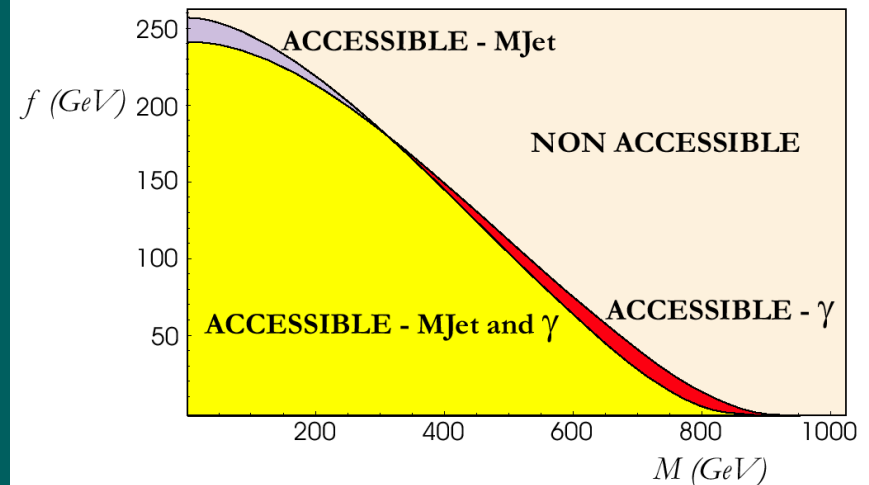
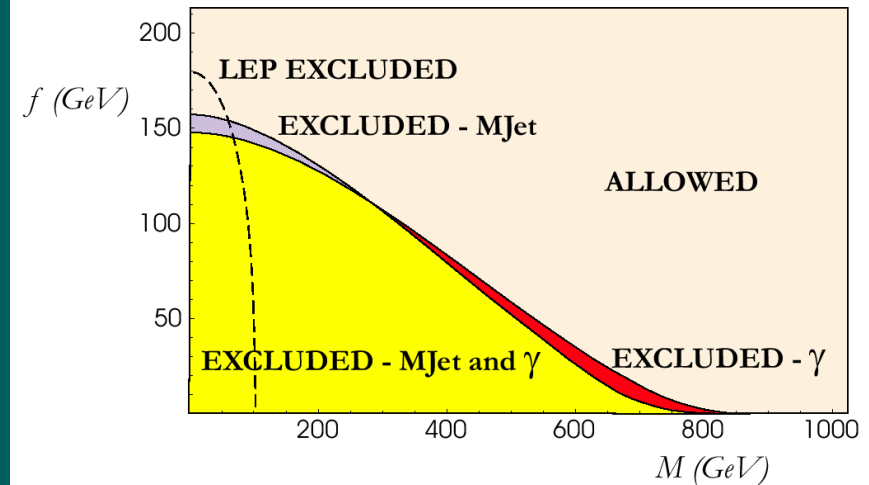
1<sup>st</sup> Run:  $E_{MC} = 1.8 \text{ TeV}$

$\mathcal{L} = 78.8 \text{ pb}^{-1}$  (D0)

$\mathcal{L} = 87.4 \text{ pb}^{-1}$  (CDF)

2<sup>nd</sup> Run:  $E_{MC} = 1.96 \text{ TeV}$

$\mathcal{L} = 1000 \text{ pb}^{-1}$



# LHC PROSPECTS

## 1.- Signals

$$\left. \begin{array}{l} \bar{q}q \rightarrow gG^{(k)}, \gamma G^{(k)} \\ qg \rightarrow qG^{(k)} \\ gg \rightarrow gG^{(k)} \end{array} \right\} \text{jets} + \cancel{E}_T, \gamma + \cancel{E}_T$$

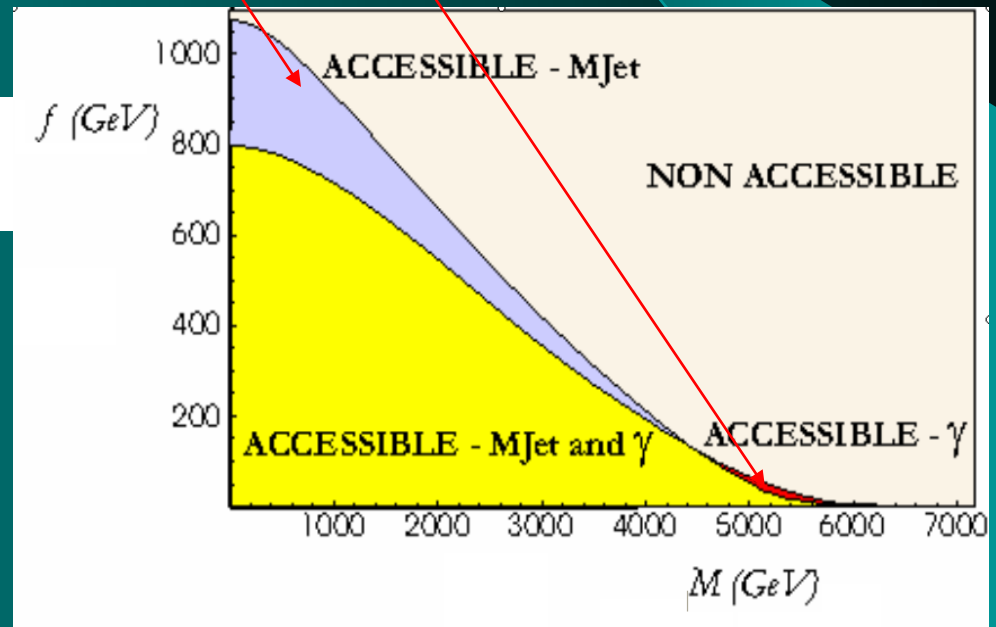
## 2.- Backgrounds

jets + ( $Z \rightarrow \nu\nu$ )  
jets + ( $W \rightarrow (\ell)\nu$ )

**Sensitivity:**

$$E_{\text{CM}} = 14 \text{ TeV}$$

$$\mathcal{L} = 10^5 \text{ pb}^{-1}$$



# BRANONS IN COSMOLOGY

---

Branons are generically stable, weakly interactive and massive.



*Weakly Interactive Massive Particles: WIMPs.*

- 1.- Branons: Dark Matter (DM) candidates.
- 2.- Searches of branons as Dark Matter.
  - 2.a.- Direct detection experiments.
  - 2.b.- Indirect detection experiments.
- 3.- Cosmological and astrophysical restrictions.

# RELIC DENSITY

The evolution of the number density follow the Boltzmann equation:

$$dn_{\text{Br}}/dt = -3Hn_{\text{Br}} - \langle \sigma_A v \rangle [(n_{\text{Br}})^2 - (n_{\text{Br}}^{\text{eq}})^2]$$

Thermal equilibrium density:

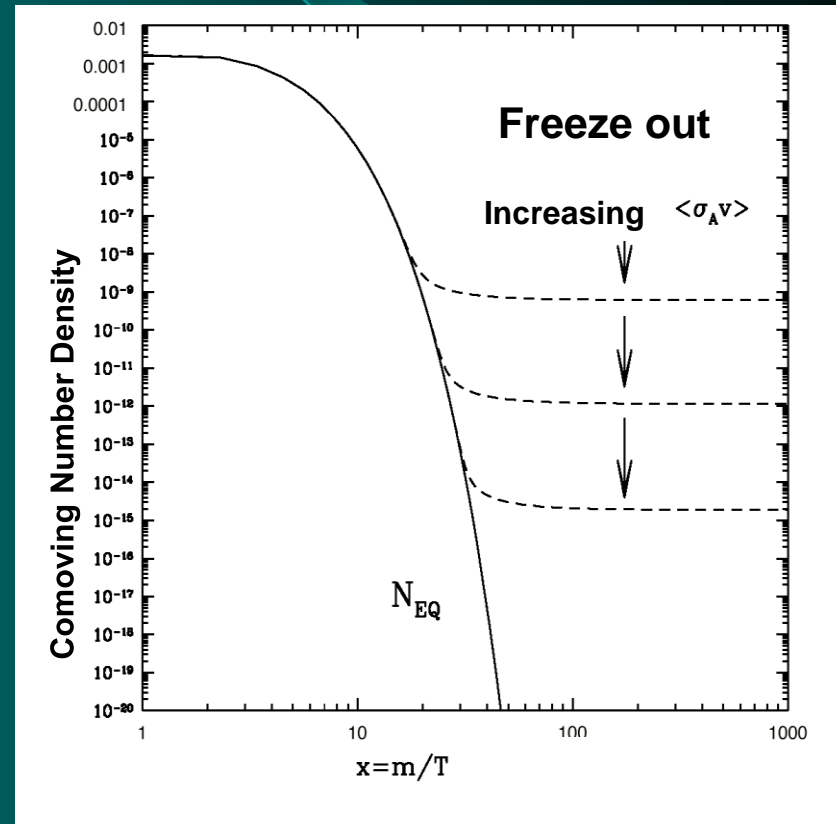
$$n_{\text{Br}}^{\text{eq}} = g/(2\pi)^3 \int f(p) d^3p$$

When  $\Gamma = \langle \sigma_A v \rangle n_{\text{Br}} < H$ , the DM is frozen out.

Cold DM relic density:  $\longrightarrow$

$$\Omega_{\text{Br}} h^2 \propto m_{\text{Br}} / \langle \sigma_A v_{\text{Br}} \rangle$$

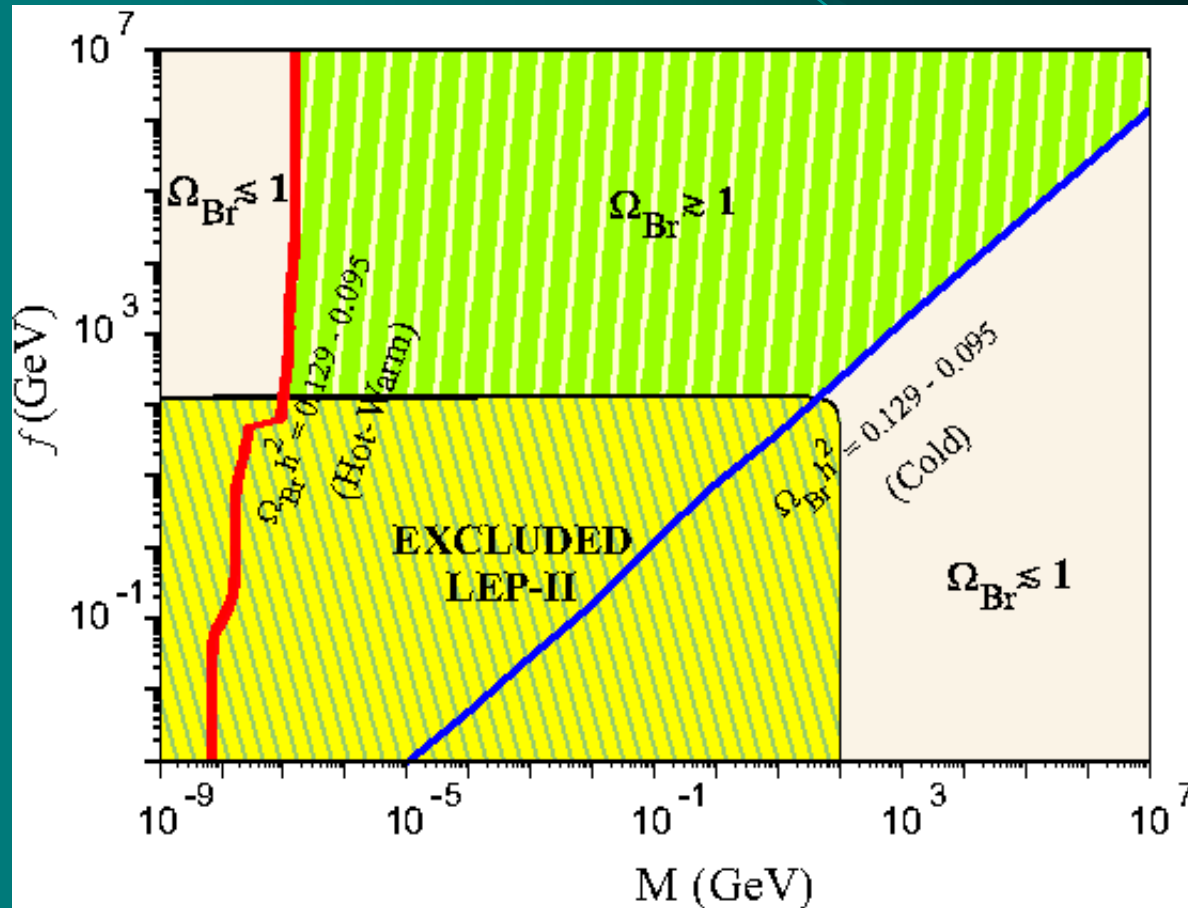
$$T_{\text{FO}} \sim m_{\text{Br}} / 20$$






# BRANON ABUNDANCE

We have taken into account the total annihilation cross section of branons to SM particles.



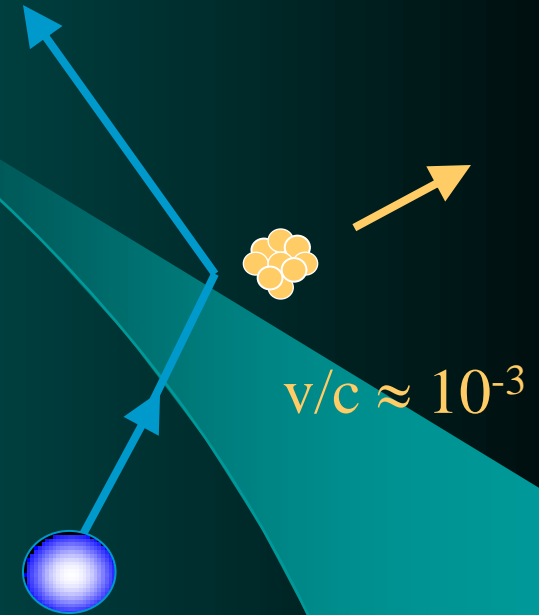
# DIRECT SEARCHES

*WIMPs* elastically scatter off nuclei

 **nuclear recoils**  
**Measure recoil energy spectrum**

Direct interaction of the DM halo with the detector. Typical nucleus recoil energy:  
 $E_R \sim 1\text{-}100 \text{ keV}$ .

The rate of the *WIMP* interactions depends on the local DM density and relative *WIMP* velocity.



# DIRECT RESULTS

The appropriate quantity to compare with the experimental results is not the elastic branon-nucleus cross section  $\sigma$ , but the differential cross section per nucleon at zero momentum transfer:  $\sigma_n$ .

$$\frac{d\sigma}{d|q|^2} = \frac{\sigma_n A^2 F^2(|q|)}{4v^2 \mu^2}$$

$F(|q|)$  is a nuclear form factor  
normalization  $F(0) = 1$

$A$  is the mass  
number of the nucleus

$$\mu = Mm/(M+m)$$

$$m \simeq 939 \text{ MeV}$$

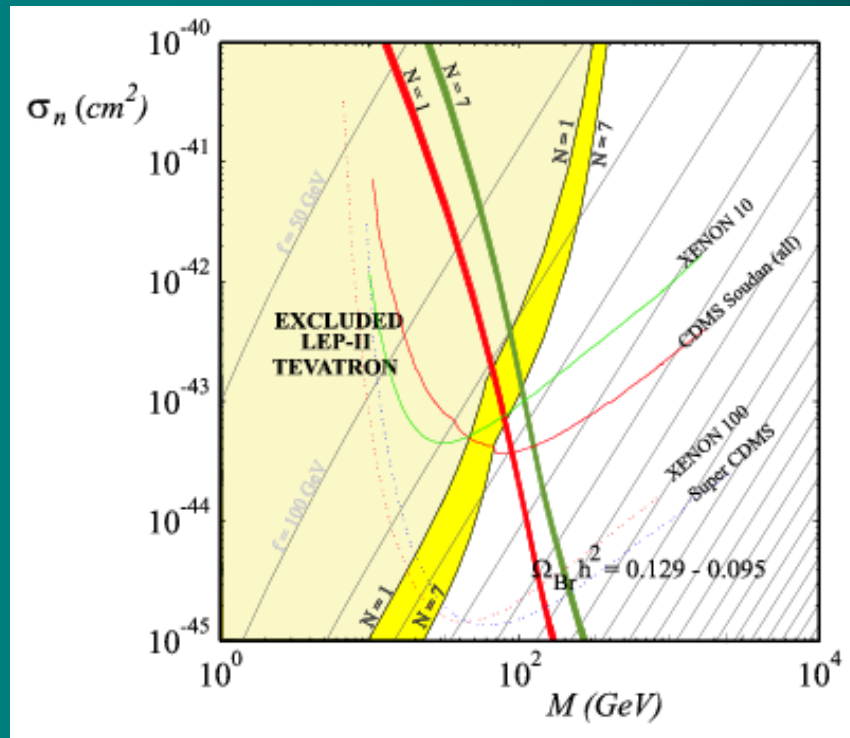
$v$  is the relative velocity

For the branon  
case:

$$\sigma_n = \frac{9M^2 m^2 \mu^2}{64\pi f^8}$$

# DIRECT RESULTS

The appropriate quantity to compare with the experimental results is not the elastic branon-nucleus cross section  $\sigma$ , but the differential cross section per nucleon at zero momentum transfer:  $\sigma_n$ .



For the branon case:

$$\sigma_n = \frac{9M^2 m^2 \mu^2}{64\pi f^8}$$

# INDIRECT SEARCHES

## *WIMPs* annihilate

1.- In the center of the Sun, and the Earth core:  
high energy neutrinos.

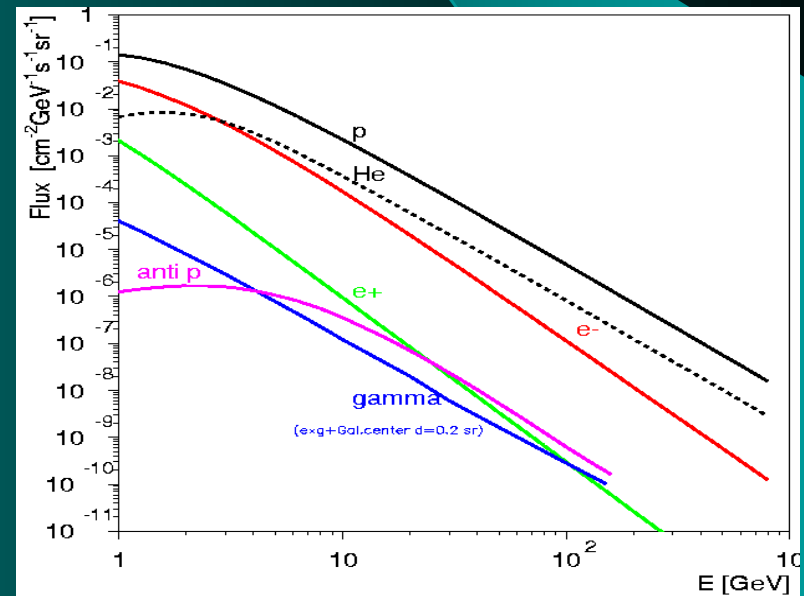
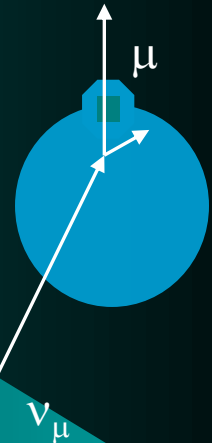
Antares, Amanda, IceCube, ...

2.- In the halo:  $\gamma$ ,  $e^+$ ,  $p^-$ ,  $D$  ...

2.a.- Halo profiles from simulations  
and rotation curves.

2.b.- Green's functions from  
propagation model.

2.c.- Average cross section from the  
effective theory.



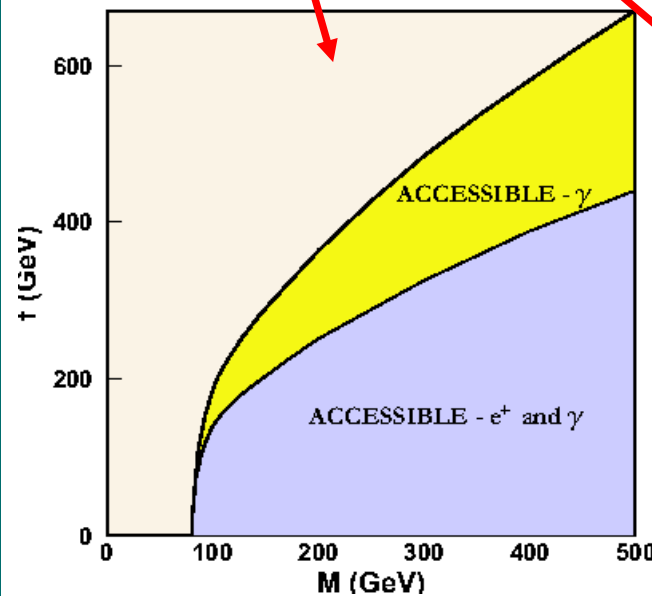
# AMS-02 PROSPECTS

Cosmic Rays : p,  
D, He, C, ...,  $e^+$ ,  $e^-$ ,  
 $\gamma$ , ...

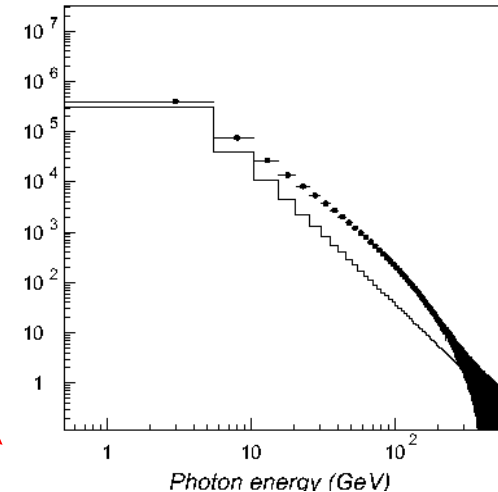
Will Collect  $\sim 10^{10}$   
CRs in Near-  
Earth Orbit from  
few GeV to few  
TeV.

## AMS estimations:

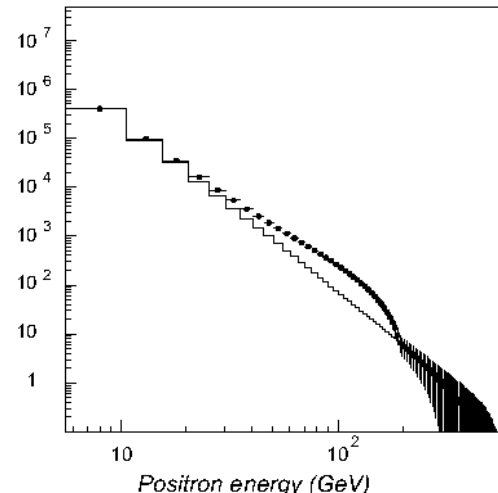
- 1.- Positrons
- 2.- Photons
- 3.- Sensitivity



Events / 5 GeV



Events / 5 GeV



# GAMMA RAY DIRECTIONS

$$\Phi_{\gamma}(\psi) = \frac{N_{\gamma} \langle \sigma v \rangle}{4\pi m^2} \times \frac{1}{\Delta\Omega} \int_{\Delta\Omega} d\Omega \int_{\text{los}} \rho^2[r(s)] ds$$

1.- Particle model dependence

2.- Astrophysical dependence

Cored Power-Law Models

$\alpha$	Sagittarius		Draco		Canis	
	$\Delta\Omega = 10^{-3}$ sr	$\Delta\Omega = 10^{-5}$ sr	$\Delta\Omega = 10^{-3}$ sr	$\Delta\Omega = 10^{-5}$ sr	$\Delta\Omega = 10^{-3}$ sr	$\Delta\Omega = 10^{-5}$ sr
0.2	0.6	3.4	0.07	2.2	2.4	3.4
0	0.6	3.3	0.06	2.2	2.4	3.5
-0.2	0.6	3.2	0.07	2.2	2.4	3.4

Cusped Models

$\gamma$	Sagittarius		Draco		Canis	
	$\Delta\Omega = 10^{-3}$ sr	$\Delta\Omega = 10^{-5}$ sr	$\Delta\Omega = 10^{-3}$ sr	$\Delta\Omega = 10^{-5}$ sr	$\Delta\Omega = 10^{-3}$ sr	$\Delta\Omega = 10^{-5}$ sr
0.5	1.1	17.8	0.1	5.7	6.2	32.3
1 (NFW)	1.3	36.9	0.1	7.2	8.3	139.9
1.5 (Moore)	7.3	615.1	0.6	55.4	49.1	5469

Galactic Center

Profile	$\Delta\Omega = 10^{-3}$ sr	$\Delta\Omega = 10^{-5}$ sr
NFW, $\gamma = 1$	26	280
Cored, $\alpha = 0$	0.3	0.3

units of  $10^{23} \text{ GeV}^2 \text{ cm}^{-5}$

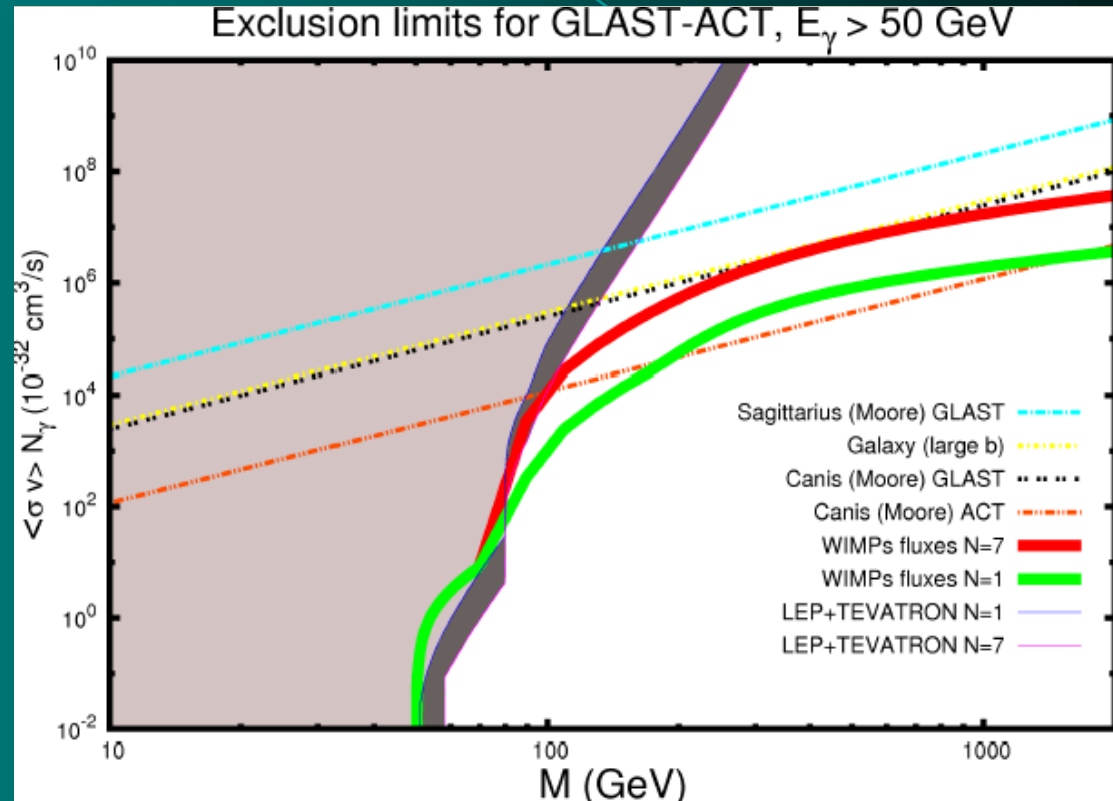
$$\rho_{\text{pow}}(r) \equiv \frac{v_a^2 r_c^\alpha}{4\pi G} \frac{3r_c^2 + r^2(1 - \alpha)}{(r_c^2 + r^2)^{2+\alpha/2}}$$

$$\rho_{\text{cusp}}(r) \equiv \frac{A}{r^\gamma (r + r_s)^{3-\gamma}}$$

(Evans, Ferrer, and Sarkar)

# GAMMA RAY DIRECTIONS

For the branon case:



(de la Cruz-Dombriz, Cembranos, Dobado, and Maroto)

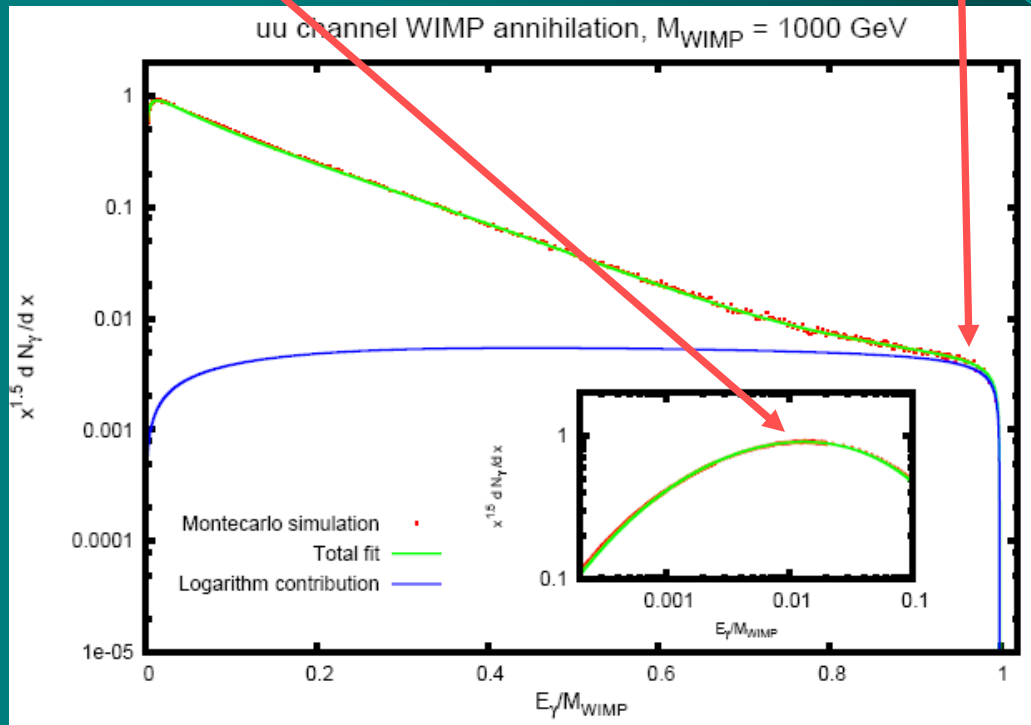


# GAMMA RAY SPECTRA

Two different strategies for a continuous spectrum:

1.- Maximum

2.- Weizsacker-Williams radiation



(de la Cruz-Dombriz,  
Cembranos, Dobado, and  
Maroto)

$$\pi(p_1)\pi(p_2) \longrightarrow e^+(k_1)e^+(k_2)\gamma_\mu(q)$$

$$x = E_\gamma/M$$

$$\left\langle \frac{d\sigma_\gamma}{dx} v \right\rangle = \frac{\alpha M^6 x \left[ 1 - \frac{m_e^2}{M^2(1-x)} \right]^{1/2}}{90 f^8 \pi^2 N} \left\{ x^2 [9(1-x) + 4x^2] + 3(1-x)[1 + (1-x)^2] \ln \frac{M^2(1-x)}{m_e^2} \right\}$$

# COSMOLOGICAL RESTRICTIONS

## 1.- Dark Matter density.

1.a. Cold Dark Matter.

1.b. Hot Dark Matter.

1.b.I.- Restrictions due to the total dark matter density.

4.b.II-. Restrictions due to the power spectrum.

## 2.- Nucleosynthesis.

## 3.- Astrophysical Observations

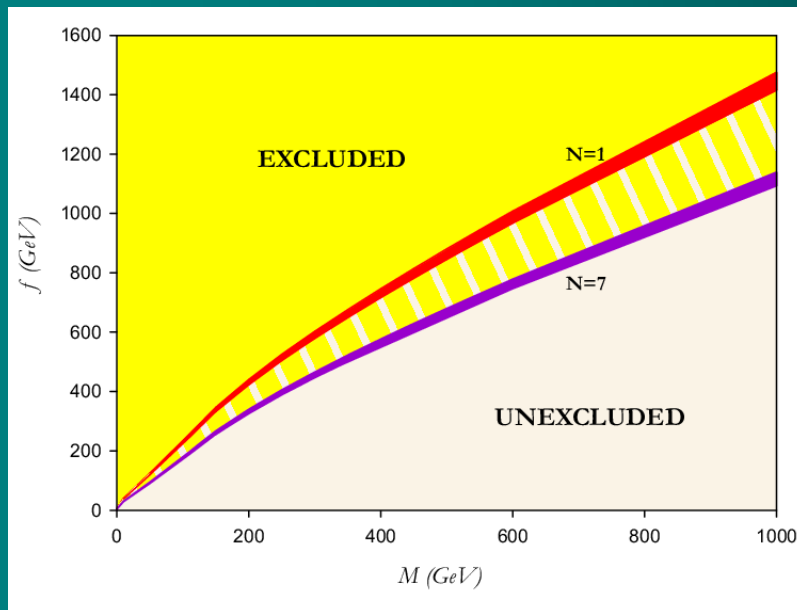
3.a. Supernova SN1987A

# TOTAL DARK MATTER DENSITY

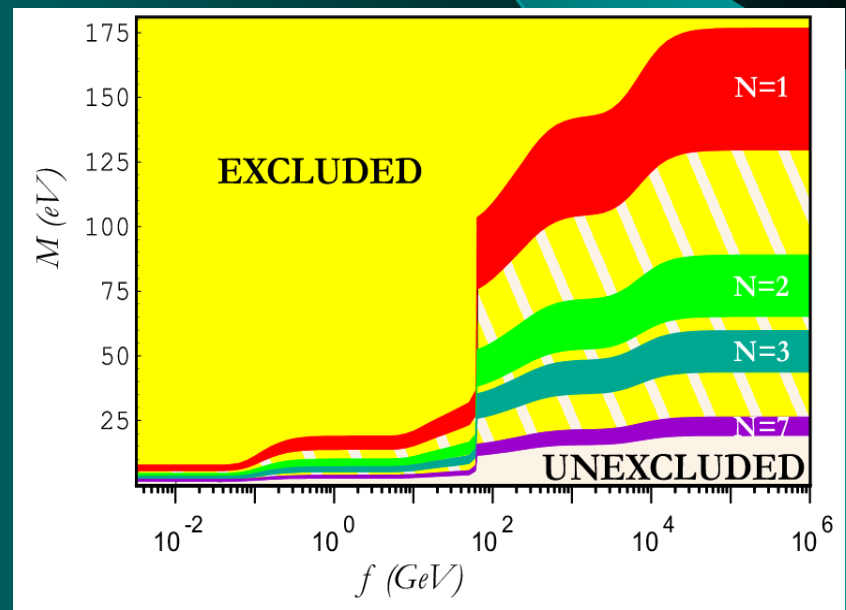
The observational bounds to the total non baryonic dark matter density coming from *WMAP* are:

$$\Omega_{\text{NBDM}} h^2 = 0.129 - 0.095 \text{ at the 95\% C.L.}$$

## Branon as Cold Relic



## Branon as Hot Relic

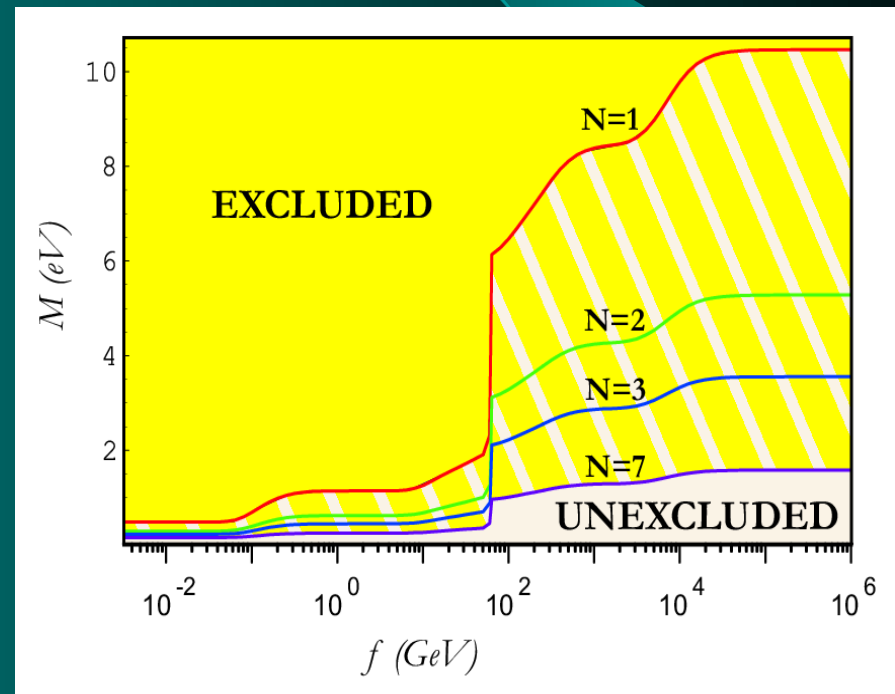


# HOT DARK MATTER DENSITY

More constraining limits on the hot dark matter energy density can be derived from a combined analysis of the data from *WMAP*, *CBI*, *ACBAR*, *2dF* and *Lyman- $\alpha$* .

$$\Omega_{\text{HDM}} h^2 < 0.0076 \text{ at the 95\% C.L.}$$

Hot dark matter is able to cluster on large scales but free-streaming reduces the power on small scales.



# NUCLEOSYNTHESIS

One of the most successful predictions of the standard cosmological model is the relative abundance of the light elements.

It is very sensitive to the number of relativistic degrees of freedom through the Hubble parameter  $H$  (rate of the Universe expansion). At a given temperature  $T$ :

$$g_{eff}(T) = g_{eff}^{SM}(T) + \sum_{\text{nuevos bosones}} g_i \left( \frac{T_i}{T} \right)^4 + \frac{7}{8} \sum_{\text{nuevos fermiones}} g_i \left( \frac{T_i}{T} \right)^4$$

An increase in the number of relativistic degrees of freedom during nucleosynthesis could deviate the predictions from the observations.

Usually, this restriction is parameterized in terms of the effective number of neutrino species:

$$N_\nu = 3 + \Delta N_\nu$$

# BBN RESTRICTIONS

Restrictions for the number of branons  $N$ :

1.- If branons decouple after nucleosynthesis:

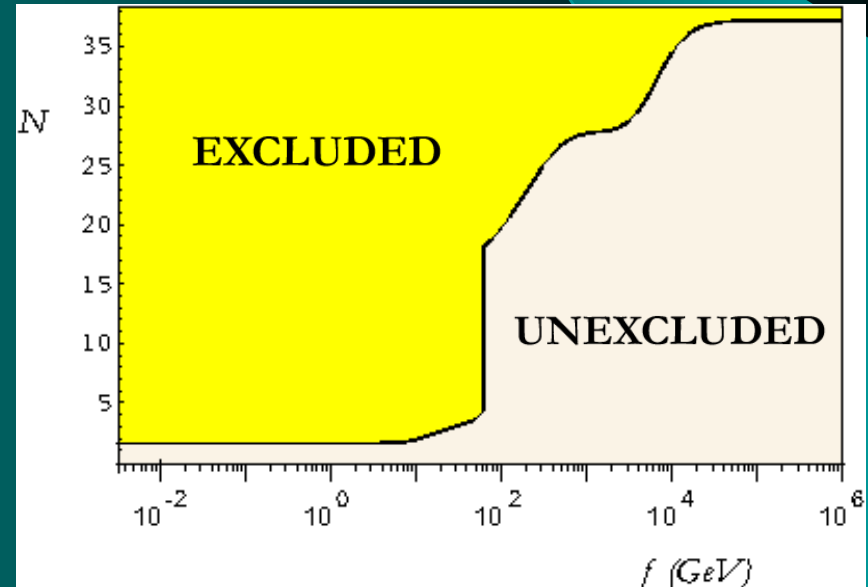
$$N \leq \frac{7}{4} \Delta N_\nu$$

2.- If branons decouple before nucleosynthesis:

$$N \leq \frac{7}{4} \Delta N_\nu \left( \frac{g_{eff}(T_{f,B})}{10.75} \right)^{4/3}$$

For example, a conservative bound for the number of effective neutrinos is:

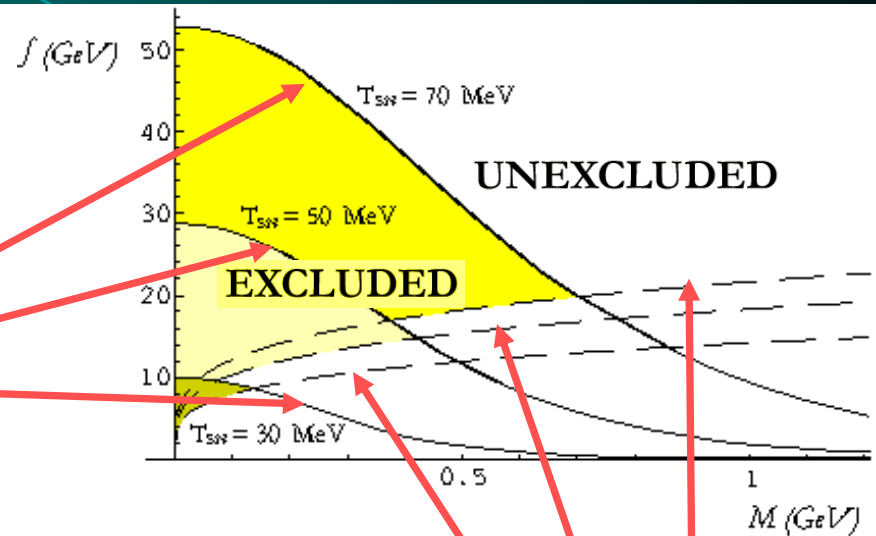
$$\Delta N_\nu = 1$$



# SUPERNOVA SN1987A

## Results for different SN1987A temperatures

$$Q \gtrsim 5 \times 10^{-30} \text{ GeV}^5$$



We estimate such energy by considering the channel corresponding to electron-positron annihilation:

$$Q_{Br}(f, M) \equiv \int \prod_{i=1}^2 \left\{ \frac{d^3 k_i}{(2\pi)^3 2E_i} 2f_i \right\} (E_1 + E_2) 2s \sigma_{e^+e^- \rightarrow \pi\pi}(s, f, M)$$

On the other hand, the mean free path should be larger than the star size

$$L \sim (8\pi f^8)/(M^2 T_{SN}^4 n_e)$$

$$R \sim \mathcal{O}(10) \text{ Km}$$

# GENERAL SITUATION

General situation of the branon physics and its cosmological interest ( $N = 1$ ):

3. - Restrictions due to the power spectrum.

2.- Restrictions due to the total dark matter density.

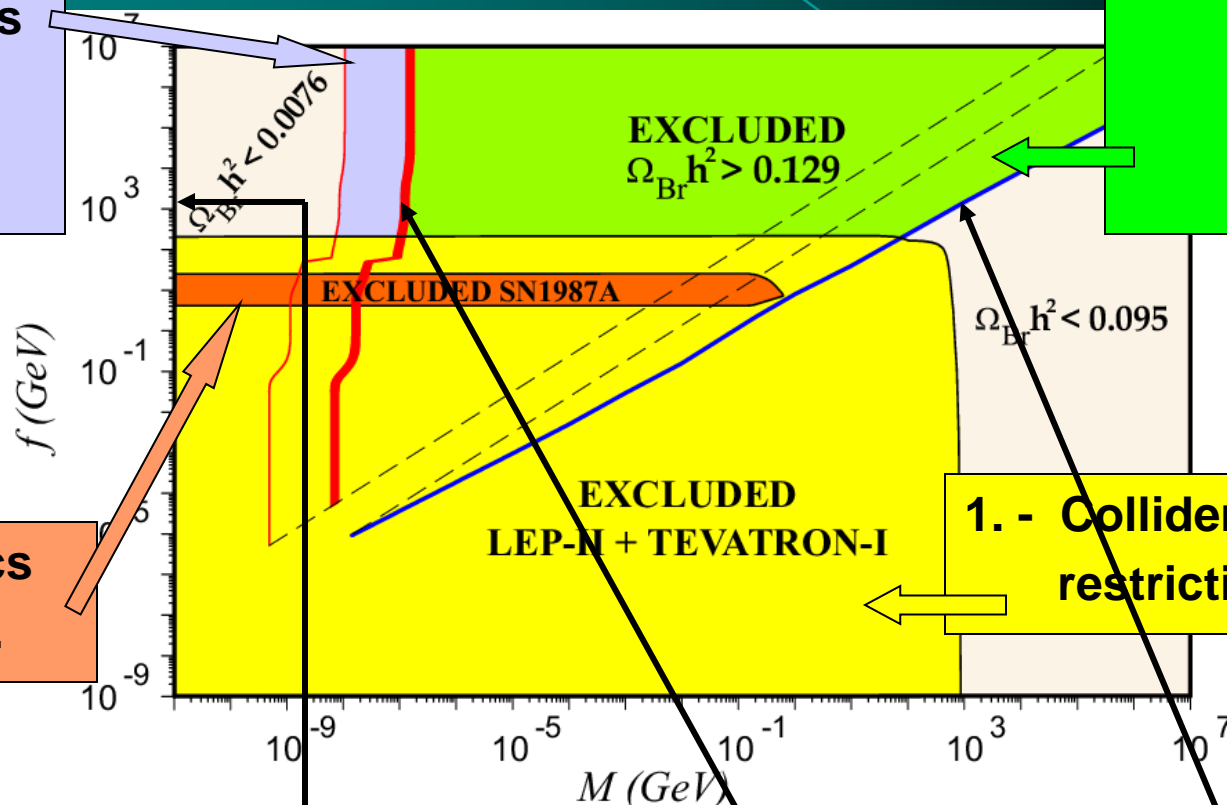
4. - Astrophysics restrictions.

1. - Collider restrictions.

C.- Branons as Non Thermal Relic

B.- Branons as Warm DM

A.- Branons as WIMPs





# RADIATIVE CORRECTIONS

Modifications in the standard model phenomenology due to branon radiative corrections:

## 1.- One loop correction

- 1.a. New effective interactions among four particles.
- 1.b. Force mediated by branons.

## 2.- Two loop corrections

- 2.a. Electroweak precision observables.
- 2.b. Muon anomalous magnetic moment.

$\Lambda$ : Scale associated with new physics.

# ONE LOOP CORRECTION

New phenomenology in particle accelerators:

$$\Gamma_L^{(2)}[\Phi] = \frac{N\Lambda^4}{192(4\pi)^2 f^8} \int dx \{2T^{\mu\nu}T_{\mu\nu} + T_\mu^\mu T_\nu^\nu\}$$

Lower bounds for the parameter:  $f^2/(N^{1/4}\Lambda)$ .

Prospects for future experiments:

	$\sqrt{s}$ (TeV)	$\mathcal{L}$ (fb $^{-1}$ )	$f^2/(N^{1/4}\Lambda)$
ILC	0.5	500	261
	1.0	200	421
Tevatron	2.0	2	83
	2.0	30	108
LHC	14	10	332
	14	100	383

# MUON ANOMALOUS MOMENT

The BAGS (Brookhaven Alternating Gradient Synchrotron) has reached a relative precision of 0.5 ppm in the determination of  $a_\mu = (g_\mu - 2)/2$ .

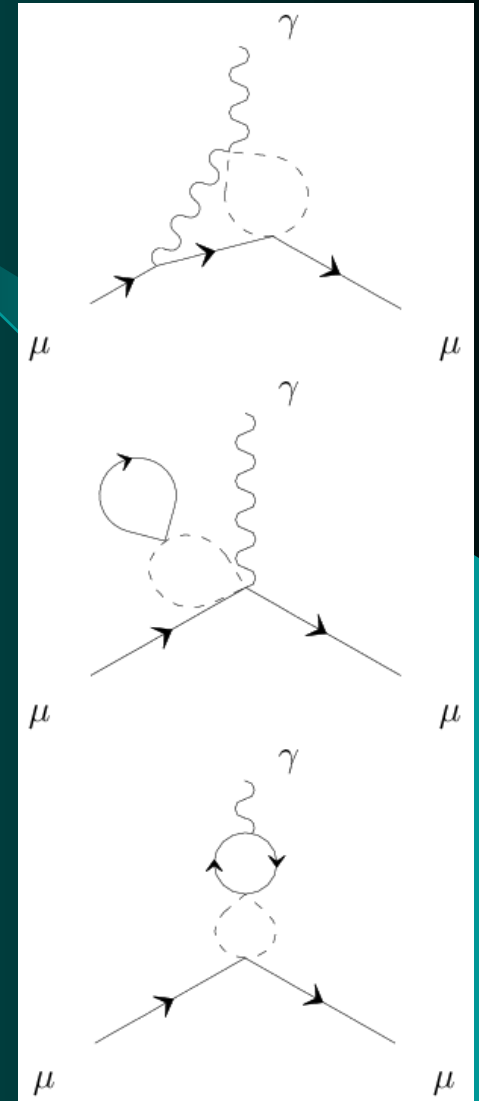
The E821 Collaboration at BAGS has found a  $2.6 \sigma$  deviation with the SM:

$$\delta a_\mu \equiv a_\mu(\text{exp}) - a_\mu(\text{SM}) = 23.5 (9.0) \times 10^{-10}$$

(Passera, Höcker)

The branon contribution to the muon anomalous magnetic moment is a two loop effect.

$$\delta a_\mu \approx \frac{5 m_\mu^2}{114 (4\pi)^4} \frac{N \Lambda^6}{f^8}$$



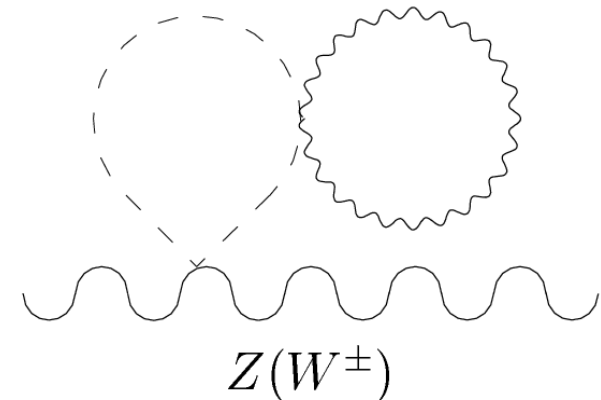
# EW PRECISION OBSERVABLES

The results of the electroweak precision tests performed at LEP and SLC form a stringent set of precise constraints to compare with new physics.

We can focus on the

parameter:  $\bar{\epsilon} \equiv \frac{\delta M_W^2}{M_W^2} - \frac{\delta M_Z^2}{M_Z^2}$

$$\delta \bar{\epsilon} \approx \frac{5 (M_Z^2 - M_W^2)}{12 (4\pi)^4} \frac{N \Lambda^6}{f^8}$$



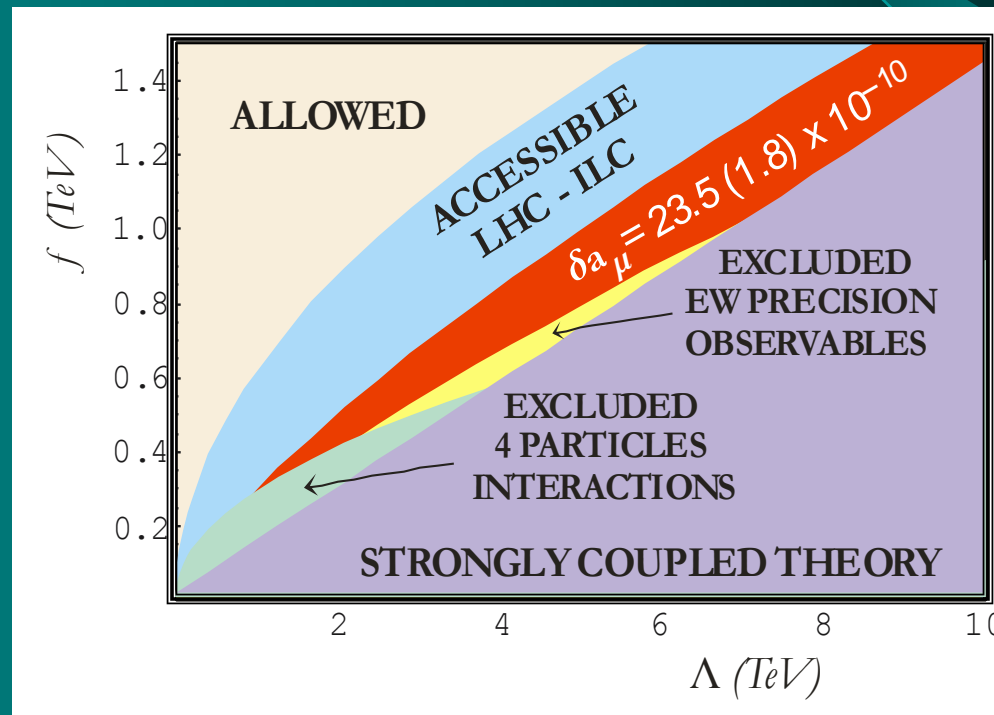
LEP and SLD result:  $\bar{\epsilon} = 12.7 (1.6) \times 10^{-3}$

(Altarelli, LEP EW Working Group)

The branon contribution to the electroweak precision observables is also a two loop effect.

# RADIATIVE RESULTS

The branon radiative effects (at 95% C.L.) on the Standard Model phenomenology can be observed in the following general plot ( $N = 1$ ):



# CONCLUSIONS

1.- The branon signals constitute the first observational evidence for some extra dimensional models:

Flexible Brane Worlds ( $f \ll M_F$ ).

2.- Their phenomenology can be determined in a model independent way in terms of the brane tension scale  $f$ , their number  $N$  and their masses  $M$ .

3.- This phenomenology is very rich and could be related with a great variety of experimental signals beyond the SM:

3.a. Scattering experiments: Single  $\gamma$ , MonoJet production, bhabha scattering ...

3.b. Cosmological observations: Dark Matter candidate ...

3.c. Astrophysical Analysis: Direct searches, Indirect searches ...

3.d. Electroweak Precision observables,

3.e. Muon anomalous magnetic moment ...



# IMPORTANT CONCLUSIONS

## 1.- Spain won



## 2.- Today (07/07) is San Fermín

